## Homework of Week 6

## Deadline: 9:00am, November 4 (Thursday), 2021

- 1. Let  $X_1, ..., X_n$  be independent and identically distributed Poisson random variables and  $X = \sum_{i=1}^n X_i$ . Let  $\mathcal{E}$  be the event that all  $X_i$ 's are nonzero. Prove that  $\Pr(\mathcal{E}|X = k)$  increases with k.
- 2. Let  $X_1, ..., X_n$  be independent and identically distributed Poisson random variables and  $X = \sum_{i=1}^{n} X_i$ . Let  $\mathcal{E}$  be the event that all  $X_i$ 's are nonzero. We know that  $\Pr(\mathcal{E}|X=k)$  increases with k. Prove that for any  $0 < k_1 < k_2$ ,  $\Pr(\mathcal{E}|X=k_1) \leq \Pr(\mathcal{E}|X \in [k_1, k_2])$ .
- 3. Do Bernoulli experiment for 20 trials, using a new 1-Yuan coin. Record the result in a string  $s_1s_2...s_i...s_{20}$ , where  $s_i$  is 1 if the  $i^{th}$  trial gets Head, and otherwise is 0.